

## Modeling IR spectra of CO<sub>2</sub> isotopologues and CH<sub>4</sub> trapped In type I clathrate

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**Abstract.** To test the hypothesis of atmospheric carbon dioxide or methane storage in metastable clathrate, a theoretical formalism is developed to model and simulate the spectra of the CO<sub>2</sub> or CH<sub>4</sub> molecule trapped in clathrates. 12-6 Lennard-Jones atom-atom potentials are used to account for short and long range interactions between the atoms of the trapped molecules and atoms of H<sub>2</sub>O molecules of the cage. Effective electric charges are used for electrostatic interactions with H<sub>2</sub>O molecules. The calculations were performed on clathrates of type I, with a small and a large cage to determine equilibrium configurations for both CO<sub>2</sub> and CH<sub>4</sub> and vibrational shifts were determined for CO<sub>2</sub> in an undistorted trapping nano-cage.

### 1 The interaction potential energy

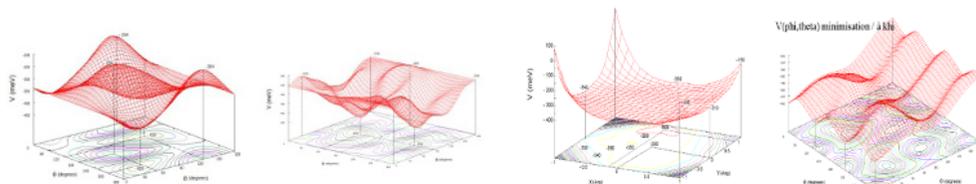
The interaction potential energy  $V_{MC}$  between the trapped CO<sub>2</sub> or CH<sub>4</sub> molecule and the rigid clathrate cage is expressed as:

$$V_{MC} = \sum_{k=1}^{N_W} \sum_{j=1}^3 \sum_{i=1}^3 4\epsilon_{ij} \left\{ \left( \frac{\sigma_{ij}}{r_{ijk}} \right)^{12} - \left( \frac{\sigma_{ij}}{r_{ijk}} \right)^6 \right\} - \frac{1}{4\pi\epsilon_0} \frac{q_i q_j}{r_{ijk}}$$

where  $i$  and  $j$  denote the  $i^{\text{th}}$  atom of the trapped CO<sub>2</sub> or CH<sub>4</sub> molecule and the  $j^{\text{th}}$  atom of the  $k^{\text{th}}$  water molecule of the clathrate matrix, separated by the distance vector  $r_{ijk}$ ; and  $\epsilon_{ij}$  and  $\sigma_{ij}$  are the mixed LJ potential parameters, obtained from the usual Lorentz-Berthelot combination rules  $\epsilon_{ij} = \sqrt{\epsilon_{ii} \epsilon_{jj}}$  and  $\sigma_{ij} = (\sigma_{ii} + \sigma_{jj})/2$ . In the second term of the above equation  $q_i$  and  $q_j$  are the electric charges of the  $i^{\text{th}}$  atom of the trapped molecule and the  $j^{\text{th}}$  atom of the water molecules.

## 2 Results of equilibrium configuration

Calculations were performed on clathrates of type I, with unit cell consisting of 2 dodecahedral cages ( $5^{12}$ ) and 6 tetrakaidecahedral cages ( $5^{12}6^2$ ), termed small and large cage respectively and results are given in Figures 1a) and 1b). The minimum configuration energy for the small cage corresponds to an interaction energy of  $-378$  meV ( $-3050$   $\text{cm}^{-1}$ ). The molecule is at the center of the cage opposite to the centers of 2 pentagonal faces and with an allowed translation motion around the center of the cage. For the large cage, energy minimum is calculated to be  $-418$  meV ( $-3375$   $\text{cm}^{-1}$ ). The molecule is parallel to the two hexagonal faces of the cage with a translational motion of large amplitude (0.07 nm) around the center of the cage in the direction parallel to the hexagons. Only librations are expected from calculations [1,2].



**Figure 1** a)  $\text{CO}_2$  in large cage b)  $\text{CO}_2$  in small cage c)  $\text{CH}_4$  in large cage d)  $\text{CH}_4$  in small cage.

For  $\text{CH}_4$ , results are given in Figures 1c) and 1d). Calculations give in the small cage a minimum potential energy of  $-405$  meV ( $-3270$   $\text{cm}^{-1}$ ).  $\text{CH}_4$  is at the center of the cage, with H atoms more or less facing pentagonal faces. In the large cage : the minimum potential energy is determined to be  $-338$  meV ( $-2730$   $\text{cm}^{-1}$ ).  $\text{CH}_4$  is not at the center of the cage and H atoms point more or less to pentagonal faces. For both cages, translational motions of large amplitudes and hindered orientational motions are expected from calculations [3].

Results in the undistorted cages show that the  $\text{CO}_2$  vibrational fundamental modes are blue shifted in the small cage and red shifted in the large one. A larger effect is shown for levels coupled by Fermi Resonance and a splitting of the degenerate vibrational mode  $\nu_2$  is expected. Preliminary results in distorted cages show only red shifts are to be expected.

## References

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