

# Drying kinetics of RDF: Experimental investigation and modeling

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**Abstract.** An experimental study was performed to determine the drying characteristics of an oversized fraction of RDF alternative fuel using a laboratory scale hot air dryer at a variety air temperatures and a constant air velocity. For this research the industrial RDF was derived from a Regional Municipal Waste Treatment Facility near the city of Kraków, Poland. The samples of RDF were prepared in two forms: oversized (unmodified condition) and shredded in a two-drum crusher. In addition, the RDF was sorted into three groups of samples: paper, plastic, textiles. Each form of RDF and each group of samples were dried in hot air dryer at temperatures of 50, 70 i 90 °C and a constant air velocity of 1,5 [m·s<sup>-1</sup>]. The loss of the the samples mass were measured in a continues manner until the equilibrium moisture content was reached. The effective moisture diffusivity [m<sup>2</sup>·s<sup>-1</sup>] and activation energies [kJ·mol<sup>-1</sup>] was amounted. The analysis of the course of moisture content change concludes that that the drying of the RDF alternative fuel occurred mainly in the II period of the process during which the transport of water content was carried out by diffusion. And, to a lesser extent, with the surface heat transfer in II period. Based on the calculated data there was a model determined which presented the best possible matching of the course of moisture content change.

## 1 Introduction

RDF alternative fuel is a combustible fraction of municipal or industrial waste obtained from the separation of the biodegradable fraction. It is typically produced in the Regional Waste Water Treatment Plant (RIPOK). RDF is a heterogeneous fuel whose main components are paper (including cardboard), plastic and textiles [1]. RDF can also be found in admixtures of inert components: glass, wood, organic parts and metals. Their presence is due to an imperfection of the municipal waste screening process. The mass fraction of individual fractions varies, depending on the installation, source of waste: Municipal Solid Waste (MSW), Commercial and Industrial Waste (CIW), Construction and Demolition Waste (CDW) and collection sites: urban and rural [2, 3, 4]. Typically, RDF is dominated by paper: 50-70%, plastic: 30-50%, textiles (<10%) and inert ingredients (<5%). An example of RDF composition according to the source of waste is presented in the Table 1.

The RDF calorific value varies between MJ·kg<sup>-1</sup> [4]. RDF humidity varies, ranging between 5-23% [3, 4]. This depends on the origin of the waste, the type of screening plant and the time of year for municipal waste collection [6, 7]. The RDF fuel surplus fraction consists of particles greater than 5 cm [8]. It is generated by screening a mechanical waste stream of municipal waste on sieve screens (drum sieves). The particle size depends

on the mesh size and typical sieve sizes are 5, 8, 10 cm [9].

RDF can be utilized thermally in combustion, pyrolysis and gasification. Most often it is a product intended for cement kilns, lime plants, waste incineration plants and power plants as well as heating plants [10]. RDF is also subjected to the process of pelleting or briquetting [11]. The moisture content parameter plays an essential role in the design and process optimisation of thermal utilisation or compaction of the RDF fuel. The presence of moisture has a great impact on the fuel's calorific value and, consequently, on the possibilities of thermal processing. For example, for a cement kiln, humidity cannot exceed 15% [12]. On the other hand, RDF with low moisture content is difficult to handle during transportation within facilities due to dust and blockages on conveyor belts. Moisture also plays a key role in the agglomeration process. Water molecules are involved in the physical-chemical reactions which occur during bonding of fuel elements (adhesion, formation of solid bridges) [13]. However, the water molecules are incompressible, which at the same time makes the compaction process quite difficult. Too high water content will result in a high relaxation coefficient [14], but too low will increase the energy efficiency of the shredding process [15] and increase the risk of spontaneous combustion as well [16]. Determining the required humidity ought to be a compromise between the

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production process and the disposal of the fuel concerned.

**Table 1.** Composition of RDF/SRF [3].

Waste component	SRF:		
	C&IW [wt%*]	CDW [wt%]	MSW [wt%]
Paper and cardboard	35.6	22.0	30.0
Plastic (soft)	24.0	6.8	19.6
Plastic (hard)	16.5	9.2	13.0
Textile	8.5	6.0	10.0
Wood	6.4	38.0	8.2
Bio Waste	-	-	0.4
Rubber	1.0	2.4	2.2
Foam	1.2	0.5	2.6
Metal	0.8	0.5	0.5
Glass	0	2.0	0.7
Stone	0	0.6	0
Fines	6.0	11.0	12.8

\* wt%=wt% percentage by weight (ratio of mass to total mass)

Thermal drying to reduce water content has been proved to be an effective method [17]. In many branches of industry, drying has a crucial role: food industry, agriculture, paper industry. There are many methods of drying available: contact, convection, microwave, radiation, dielectric and others [18]. Drying consists by removing moisture from the material through evaporating water, with the share of heat supplied to this process. The most common and simplest method is drying by convection using gas, usually warm air, as a drying medium. In this process, the transport of heat and mass from the interior of the material to its surface is carried out by diffusion, and further on into the surrounding atmosphere by convection. Drying also can be a part of the process, taking part in the preparation of the raw material for the compaction process of solid biofuels [19], and yet is a very energy consuming process. Since RDF is a heterogeneous material composed of many different components, it contains different types of moisture. The paper and textiles would probably be the main water binding materials in alternative fuel [20]. The water contained there would be primarily capillary bounded, while in the plastics the moisture would be collected as a film on the surface. The RDF is a lightweight, porous and bulky material, so convective drying would have a more practical effect due to the ease of flow of the drying medium between the RDF elements. Knowing the drying kinetics has a key role in designing and optimization for the agglomeration or thermochemical processing of raw materials [21]. There are articles concerning drying of paper, paper sludge [i.e. 22, 23, 24], textiles [25] or food waste [26]. These research studies focused on drying kinetics analysis, drying curves analysis, the Effective moisture diffusivity ( $D_{eff}$ ) and Activation energies ( $E_a$ ) determinations and calculations the best equation for the

drying process under variable factors (i.e. temperature of drying, air velocity, initial moisture content of the sample). However very little is said in the literature concerning RDF drying. The purpose of this study is to observe the effect of various temperatures at convection drying on the drying kinetics of RDF and its main fractions (plastic, textiles and paper) in separation.

## 2 Material and methods

RDF was collected from the RIPOK industrial plant located in Krakow, which was produced from municipal solid waste sorted out of the Krakow area. The analysed fraction was formed on drum sieve with a 10 cm mesh screen installed. Because of that the RDF is mainly composed of large particles (over 3 cm).

**Table 2.** Composition of presented RDF [27].

Waste component	wt%
plastics	87.44
paper, wood and similar	5.09
textiles	2.60
biomass	1.56
glass	0.64
metal	0.49
hazardous waste	0.00
other, non-combustible	2.17

\* wt%=wt% percentage by weight (ratio of mass to total mass)

There were five types of samples prepared for the experiment:

- RDF0 – primary fine fraction gained directly from RIPOK
- RDF1 –primary fraction, shredded in a two-drum crusher on the RDF pelletizing line.

In addition, three groups of raw materials were selected from RDF0: paper, plastic and textiles.



**Fig. 1.** Samples of RDF: A) RDF1, B) RDF0.

There were samples of 12 g ( $\pm$  5 g) prepared from all raw materials for drying. Samples were dried by convection in the laboratory drier Elkon KBC 65G. The measurement stand diagram is shown in Fig. 2. The drying experiments were performed at 50, 70 i 90 °C air temperatures. The drying air velocity was at a constant 1.5 m·s<sup>-1</sup>. All the experiments were replicated five times at each temperature value for each sample type.

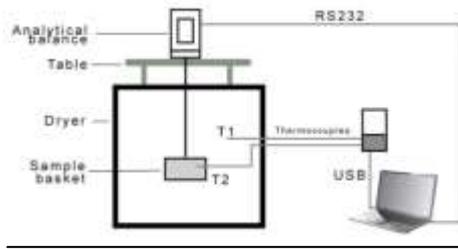


Fig. 2. Measurement stand.

The weight loss was measured by Radwag AS-160.R2 analytical balance ( $d=0,01$  mg). The measurement was recorded continuously of at 5 s interval and saved by the Radwag „Pomiar-Win” software each time. The temperature was measured with two NiCrNiAl thermocouples that were placed inside dryer. With a thermometer that Works in connection with the YC-747UD meter the temperature of the ambient environment- the inside of the dryer (T1) and the temperature of the sample (T2) was measured. The measurements were recorded continuously at 1 s intervals by Temp Monitor\_S2 (ver. 1.0.16) software. The drying proces proceeded until the moisture content reached an equilibrium value (until there were no significant variations in the moisture lost). The mean drying time was 25 minutes. A Pol-Eko SLW-53 TOP dryer was used for the samples initial moisture content measurment according to the PN-EN 15414-3:2011 standard [28]. The dry matter calculations were done according to the PN-EN ISO 638:2008 standard [29].

The moisture content ( $U_\tau$ ) was calculated from the following equation:

$$U_\tau = \frac{m_\tau - m_{db}}{m_{db}} \quad (1)$$

Where,  $m_\tau$  is the mass of the sample at any given time  $\tau$ , [kg];  $m_{db}$  the mass of the dry basis of the sample, [kg]. The unit of the moisture content is ( $U_\tau$ ) kg water/kg dry basis.

The drying rate ( $dU/dt$ ) [kg water/kg d.b.·s<sup>-1</sup>] was obtained from the following equation [18]:

$$\frac{dU_\tau}{d\tau} = \frac{U_i - U_{i+1}}{\tau_i - \tau_{i+1}} \quad (2)$$

Where  $U_i$  is the moisture content at  $i$ th time [kg water/kg d.b.],  $U_{i+1}$  is the moisture content at the  $i+1$ -th time [kg water/kg d.b.],  $\tau_i$  and  $\tau_{i+1}$  is respectively  $i$ th and  $i+1$ -th time of the measurement [s].

The three common models were used to quantify drying kinetics of RDF0 and RDF1. The models are described with simplified equations respectively [18]:

- Henderson-Pabis:

$$MR = (U_\tau - U_e) \cdot (U_i - U_e)^{-1} = a \exp(-k\tau) \quad (3)$$

- Lewis:

$$MR = (U_\tau - U_e) \cdot (U_i - U_e)^{-1} = \exp(-k\tau) \quad (4)$$

- Page:

$$MR = (U_\tau - U_e) \cdot (U_i - U_e)^{-1} = \exp(-k\tau^N) \quad (5)$$

Where,  $MR$  is the moisture ratio (dimensionless),  $U_\tau$  is the moisture content at Any given time  $\tau$  [kg water/kg d.b.],  $U_i$  is the initial moisture content [kg water/kg d.b.],  $U_e$  is the equilibrium moisture content [kg water/kg d.b.],  $k$  is the drying rate constant [s<sup>-1</sup>].  $N$  and  $a$  are the empirical constants.

Taking the natural log of both sides of the equations 3-5 is a way to determine the empirical constants. The form of the normalized equations of the moisture ratio versus time is:

- Henderson-Pabis:

$$\ln(MR) = \ln(a) - k\tau \quad (6)$$

- Lewis:

$$\ln(MR) = -k\tau \quad (7)$$

- Page:

$$\ln[-\ln(MR)] = \ln(k) + N \ln(\tau) \quad (8)$$

The Effective moisture diffusivity ( $D_{eff}$ ) [m<sup>2</sup>·s<sup>-1</sup>] can be determined from the slope of the normalized plot of the unaccomplished moisture ratio,  $\ln(MR)$  vs time, using the following equation [31]:

$$D_{eff} = -(4L^2 \cdot \pi^2) \cdot k \quad (9)$$

Where,  $L$  is the thickness of the sample (slab) of 0,0045m [m],  $k$  is the drying rate constant [s<sup>-1</sup>].

The Activation energies ( $E_a$ ) [kJ·mol<sup>-1</sup>] was obtained from the reliance of the effective moisture diffusivity  $D_{eff}$  on the temperature  $T$ . The reliance can be described by an Arrhenius type equation [31]:

$$D_{eff} = D_0 \exp\left(-\frac{E_a}{R_C \cdot T}\right) \quad (10)$$

Where the  $D_{eff}$  is effective moisture diffusivity [m<sup>2</sup>·s<sup>-1</sup>];  $D_0$  is the pre-exponential factor of the Arrhenius equation [m<sup>2</sup>·s<sup>-1</sup>],  $R$  is the universal gas constant (8.3145 kJ·mol<sup>-1</sup>·K<sup>-1</sup>) and  $T$  is the absolute air temperature [K]. Taking natural logarithm of both sides of Eq. (5) the result can be written as:

$$\ln(D_{eff}) = \ln(D_0) - \frac{E_a}{R_C} \cdot \frac{1}{T} \quad (11)$$

The activation energy ( $E_a$ ) is determined by plotting the natural logarithm of  $D_{eff}$  ( $\ln D_{eff}$ ) versus reciprocal of the absolute temperature  $T$  [K].

The experimental drying data was tested to find the most suitable model among the above mentioned (3-5). The different constants in the considered models were determined using a linear regression procedure. The adjusted coefficient of determination ( $R^2$ ), reduced chi-squared ( $\chi^2$ ) and root mean square error (RMSE) were used to inspect the goodness of fit. [18]. The matemathematical model is more suitable for higher values of  $R^2$  and lower values of  $\chi^2$ , RMSE and %E. The

following equations were used to calculate the above mentioned parameters:

$$R^2 = 1 - \frac{\sum(MR_P - \overline{MR_E})^2}{\sum(MR_E - MR_P)^2} \quad (12)$$

$$\chi^2 = \frac{\sum(MR_E - MR_P)^2}{N - n} \quad (13)$$

$$RMSE = \sqrt{\frac{\sum(MR_P - MR_E)^2}{N}} \quad (14)$$

Where  $MR_P$  is the predicted moisture ratio at any time,  $MR_E$  is the experimental moisture ratio at any time,  $\overline{MR_E}$  is the average experimental moisture ratio,  $N$  is the number of observations,  $n$  is the number of constants in the drying model.

The calculations and statistical data analysis were performed using R Core Team (2016) software (R Foundation for Statistical Computing, Vienna, Austria. URL <https://www.R-project.org/>) with the packages: ggplot, dplyr, stats.

### 3 Results and discussion

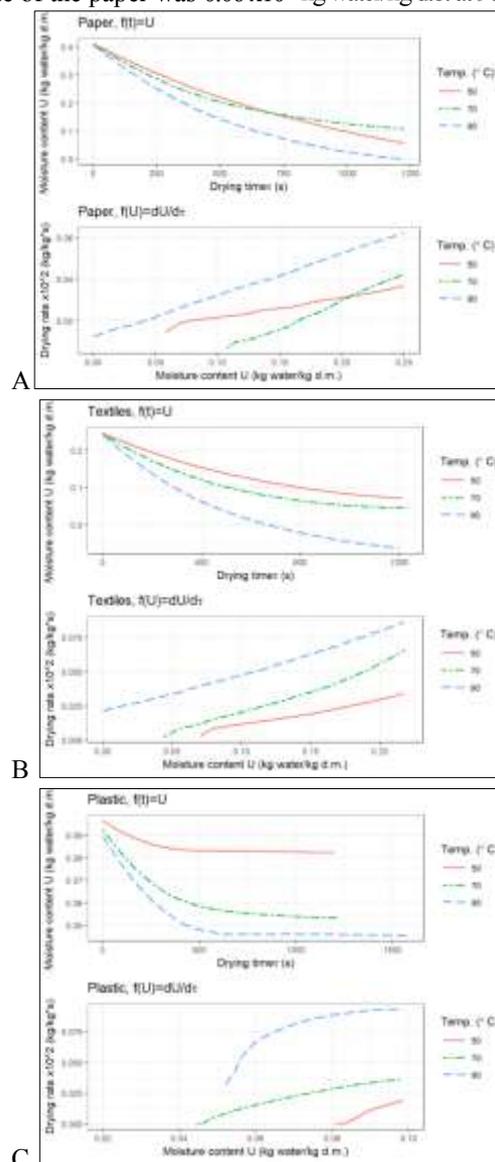
The initial moisture content of all samples were determined using PN-EN 15414-3:2011 standard [29]. As expected the highest average value of moisture content was obtained for paper (~41%) and textiles (~25%). The plastics, that were the main component of the RDF had a moisture content of approximately 10%. There was no significant difference in the moisture content values between RDF0 and the RDF1 samples. It is clear that the mechanical comminution at the pellet production line had little impact on moisture loss in the material. (Table 3).

**Table 3.** Moisture content [%] of the specific samples:

Sample	Moisture Content [%]
RDF1	21.9057
RDF0	19.1831
Plastic	9.8426
Paper	41.1430
Textiles	24.7662

The shapes of the drying curves versus time for the samples resembled the exponential function ( $U_t$ ). The steeper the curve was, the quicker the moisture loss took place. It is clearly evident that these curves were influenced by various temperatures (Fig. 3, 4). The deviations were related to the individual characters of particular samples which could be also noticed in the shapes of the moisture ratio curves (Fig. 3. – bottom plots). There was no I period of drying process in the paper and textiles. In these samples the drying process began in the second period in which the diffusion mechanism is predominant, and which is mostly common for porous matter. The drying rate was going slow at the temperature of 50 °C in the paper, however at

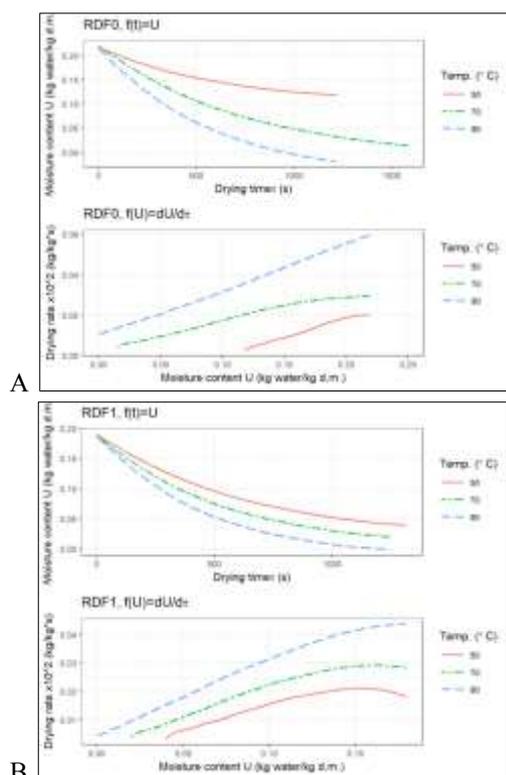
the temperature of 70 and 90 °C the rate of changes were faster (Fig. 3A, the bottom plot). The maximum drying rate of the paper was  $0.06 \times 10^{-2}$  kg water/kg d.b. at 90 °C.



**Fig. 3.** Effect of drying air temperature and moisture content on the drying rate of A) paper, B) textiles, C) plastic.

Considering the textiles, the drying curves are also noticeably influenced by the various temperatures. With the decrease of water content, the drying curves are less steep. (Fig. 3B). The paper and textiles were dried completely at the  $U = 0$  at the temperature of 90 °C after 20 minutes (1250 s). With the decrease of the temperature the final water content in the both of samples was equal to equilibrium moisture content. The maximum drying rate of the textiles was  $0,088 \times 10^{-2}$  kg water/kg d.b. at 90 °C.

Different kind of curve shapes can be observed in plastic (Fig. 3C). With the decrease of water content, the drying curves are less steep, and more flat and parallel to the x axis. There are two periods of drying



**Fig. 4.** Effect of drying air temperature and moisture content on the drying rate of A) RDF0, B) RDF1.

process in plastic, where I period is mild and long, and the II one is dynamic and short (especially at the temperature of 90 °C). This is characteristic for porous-capillary and porous materials. The maximum drying rate in plastic is  $0,085 \times 10^{-2}$  kg water/kg d.b. at 90 °C. The time of drying of 20-25 minutes is too short to

remove the water completely from the samples above at 50 °C, in particular for paper and textiles. The plastic and paper exhibit characteristics of hygroscopic material at the lower temperature values, however at 90 °C the samples exhibit the characteristics close to non-hygroscopic material [32].

Based on the shapes of the drying RDF0 and RDF1 curves it can be stated that the samples resemble capillary-porous and porous materials. The shape of the curves exhibit the characteristic of paper and textiles drying curves, although the total percentage of them didn't exceed 15 %. However the drying rate was twice more dynamic in RDF0 and RDF1 than in paper and textiles. The first period of drying, related to the constant drying rate occurred in both of RDF samples, but it lasted a short time at the temperature 50 and 70 °C. At the 90 °C the first drying period occurred slightly in RDF1, but hardly in RDF1 (Fig. 4 – bottom plots of A and B). The first drying period was specific to the plastics only (Fig. 3C), which is the main component of the RDF (ok. 70 %). The drying rate of RDF was faster in the shredded fraction (RDF1), where the area of of evaporation was larger due to reduction of particie size. At the 90 °C both of RDF samples were dried completely until the moisture content of  $U=0$  (Fig 4, bottom plots of A and B). At the lower temperatures the RDF resembled more party-hygroscopic material [9], it might contain the areas of a different moisture component. At lower temperatures RDF was dried to an equilibrium moisture content, which was 0.110 kg water/kg d.b. at  $T=50$  °C and 0.001 kg water/kg d.b. at  $T=70$  °C for RDF0, and 0.041 kg water/kg d.b.  $T=50$  °C i 0.010 kg water/kg d.b.  $T=70$  °C for RDF1 respectively.

**Table 5.** Empirical constants of the Henderson-Pabis, Levis and Page equations of RDF0 and RDF1.

Sample	Temp (°C)	Henderson-Pabis equation			Levis equation		Page equation		
		k [s <sup>-1</sup> ]	a	R <sup>2</sup>	k [s <sup>-1</sup> ]	R <sup>2</sup>	k [s <sup>-1</sup> ]	N	R <sup>2</sup>
RDF0	50	$-4.93 \times 10^{-3}$	0.9238	0.9696	$-5.90 \times 10^{-3}$	0.9239	$5.57 \times 10^{-3}$	0.6617	0.9879
	70	$-1.68 \times 10^{-3}$	1.0982	0.9907	$-1.59 \times 10^{-3}$	0.9937	$2.47 \times 10^{-3}$	0.9254	0.9910
	90	$-4.10 \times 10^{-3}$	1.5709	0.7031	$-1.59 \times 10^{-3}$	0.6598	$4.28 \times 10^{-3}$	0.9312	0.9682
RDF1	50	$-1.23 \times 10^{-3}$	0.0123	0.9950	$-1.13 \times 10^{-3}$	0.9941	$3.96 \times 10^{-3}$	0.8304	0.9934
	70	$-1.83 \times 10^{-3}$	0.9785	0.9997	$-1.86 \times 10^{-3}$	0.9992	$5.61 \times 10^{-3}$	0.8272	0.9890
	90	$-3.92 \times 10^{-3}$	1.5876	0.7152	$-3.36 \times 10^{-3}$	0.9287	$3.98 \times 10^{-3}$	0.9505	0.9808

**Table 6.** Model prediction evaluation for the RDF0 and RDF1.

Sample	Tem p (°C)	Henderson-Pabis model			Levis model			Page model		
		RMSE	$\chi^2 \times 10^{-3}$	%E	RMSE	$\chi^2 \times 10^{-3}$	%E	RMSE	$\chi^2 \times 10^{-3}$	%E
RDF0	50	0.0221	4.921	2.50	0.0349	1.228	4.496	0.0139	0.195	1.8200
	70	0.0253	6.440	5.32	0.0201	4.322	4.197	0.0249	0.621	11.583
	90	0.1523	23.434	47.89	0.1630	26.711	62.73	0.0498	2.493	54.701
RDF1	50	0.0157	0.25	2.49	0.0170	0.291	3.480	0.0181	0.327	4.414
	70	0.0046	0.002	1.18	0.0069	0.005	1.523	0.0259	0.677	9.140
	90	0.1453	0.021	37.01	0.0633	4.008	42.811	0.0378	1.278	47.30

Based on the results of the experiment the three mathematical drying models were fit to the experimental data. The calculations are revealed in Table 5 and Table 6. All of the models provided are a very good fit to the experimental data of drying RDF samples at various temperatures. Of all the models tested, the Page model offered the highest value for  $R^2$ . However, the Henderson-Pabis and Levis models had a great fit at the temperatures of 50 and 70 °C as well. At the temperatures of 50-70 °C the value of  $R^2$  parameter with the Levis model reached above 0,98 for RDF0 and RDF1 samples (Table 5). The  $\chi^2$  test values reflect to the goodness of model fit and are low (less than 0.02), but quite varied depending on samples types and the temperature of process in all three models (Table 6). The lowest  $\chi^2$  test values were obtained from the Page model. The highest values of the  $\chi^2$  test were related to the lowest values of  $R^2$  parameter and concerned the Henderson-Pabis and Levis models for modeling of drying RDF0 and RDF1 at 90 °C.

The highest values of %E parameter were obtained at the temperature 90 °C, where they reached even 62% (Table 6). The drying ratio curve of RDF1 and RDF0 at 90 °C was more linear (Fig. 4 A,B) and its deviation from values of lower temperatures probably was caused by describing it with exponential equations. Compared to RDF0, the values of %E were lower in the RDF1 sample. Maybe from the comminuted sample, which RDF1 was, more homogeneous samples were acquired.

**Table 7.** Effective diffusivities for the RDF0 and RDF1.

Sample	Temp [°C]	$D_{\text{eff}}$ [ $\text{m}^2 \cdot \text{s}^{-1}$ ]	$E_a$ [ $\text{kJ} \cdot \text{mol}^{-1}$ ]
RDF0	50	$4.0457 \times 10^{-7}$	52.07
	70	$13.7892 \times 10^{-7}$	
	90	$33.6521 \times 10^{-7}$	
RDF1	50	$10.0707 \times 10^{-7}$	28.26
	70	$15.0547 \times 10^{-7}$	
	90	$32.1453 \times 10^{-7}$	

The raise in effective moisture diffusivity  $D_{\text{eff}}$  was related to increasement of the temperature and decrease of the particle size of the samples. At 50 °C in RDF1 was almost two times higher than in RDF0 and was about  $10.0707 \times 10^{-7}$  [ $\text{m}^2 \cdot \text{s}^{-1}$ ] (Table 7). The activation energy ( $E_a$ ) for diffusion calculated from the slopes of normalized equation of  $D_{\text{eff}}$  (10) was found to be 52.07  $\text{kJ} \cdot \text{mol}^{-1}$  for RDF0 and 28.26  $\text{kJ} \cdot \text{mol}^{-1}$  for RDF1. Comminution of the RDF resulted in a decrease in activation energy.

## 4 Conclusions

1) The paper and textiles had the highest moisture content in RDF composition of 41% and 22% respectively. Moisture content of the plastic did not exceed 10 %. The comminution of RDF caused

insignificant difference in the moisture content between RDF0 and its shredded form of RDF1.

2) Based on the analysis of the drying kinetics of the RDF0 and RDF1 it could be stated that RDF has more features of porous material than porous-capillary. The first period of drying occurred only in plastic and slightly in RDF0 and RDF1 at lower drying temperatures of 50 and 70 °C. The drying process began with second period of drying in paper and textiles. The moisture and mass movement was mainly by diffusion and less by capillary action.

3) Of all of the three drying kinetics models of RDF tested, the Levis model had the best fit to the experimental data. The obtained values for  $R^2$  were greater than 0.98 and  $\chi^2$  test values were in the range of  $0.3 - 2,4 \times 10^{-3}$ . None of the mathematical models were able to satisfactorily describe the performance of drying RDF at the temperature of 90 °C.

4) The Effective moisture diffusivity ( $D_{\text{eff}}$ ) values were affected by increasing temperature. The highest values of  $33.6521 \times 10^{-7} \text{ m}^2 \cdot \text{s}^{-1}$  were obtained at 90 °C, and the lowest of  $4.0457 \times 10^{-7} \text{ m}^2 \cdot \text{s}^{-1}$  were obtained at 50 °C for RDF0. The Activation energy ( $E_a$ ) varied from 28.26  $\text{kJ} \cdot \text{mol}^{-1}$  to 52.07  $\text{kJ} \cdot \text{mol}^{-1}$  for RDF1 and RDF0 respectively. The lower energy is needed to remove water from comminuted RDF.

5) Drying process of the RDF using hot air at the temperature of 90 °C allows for removal of the moisture content completely, until  $U = 0$ . At lower temperatures of 50 °C and 70 °C the RDF could be dried until the equilibrium moisture content.

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## Nomenclature

$E_a$	activation energy, $\text{kJ} \cdot \text{mol}^{-1}$
$D_{\text{eff}}$	effective moisture diffusivity, $\text{m}^2 \cdot \text{s}^{-1}$
$D_0$	pre-exponential factor of the Arrhenius equation, $\text{s}^{-1}$
d.s.	dry solid
k	drying rate constant, $\text{s}^{-1}$
MR	moisture ratio (dimensionless)
N	number of observations
$U_\tau$	moisture content at any time, kg water/ kg d.s
$U_i$	initial moisture content (dry basis), kg water/kg d.s.
$U_e$	equilibrium moisture content, kg water/ kg d.s
T	absolute temperature, K
$\tau$	time, s

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